Supporting information for:

Efficiency of eclogite removal from continental lithosphere and

its implications for cratonic diamonds

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1. MODEL PARAMETERS

Temperature dependent thermal conductivities

Crust (Whittington et al., 2009):

$$k(T < 846K) = 2700 * \frac{199.5 + 0.0857 * T - 5 * 10^6 * T^{-2}}{0.21178} * \frac{(567.3 * T^{-1} - 0.062)}{10^6}$$

$$k(T > 846K) = 2700 * \frac{229.32 + 0.0323 * T - 47.9 * 10^{-6} * T^2}{0.22178} * \frac{(0.732 - 1.35 * 10^{-4} * T)}{10^6}$$

Mantle (McKenzie et al., 2005):

$$k(T) = \frac{5.3}{1 + 0.0015 * (T - 273)} + 1.753 * 10^{-2} - 1.0365 * 10^{-4} * T + 2.2451 * 10^{-7} * T^{2}$$
$$- 3.4071 * 10^{-11} * T^{3}$$

	²³⁵ U	²³⁸ U	²³² Th	40 K	Present Heat Production
	(ppm)	(ppm)	(ppm)	(ppm)	(µW m-3)
Bulk continental crust	$4.9*10^{-3}$	0.70	3.0	1.2	0.51
Lithospheric mantle	$2.6*10^{-4}$	0.037	0.14	0.043	0.028

Radiogenic heat production in cratons (calculated based on Rudnick et al., 1998)

The continental crust is divided into upper, middle, and lower one thirds, with 60%, 34%, and 6% of total crust heat production, respectively.

Dislocation creep constants (Jain et al., 2019)

Model OL-DB₂ for dry diffusion and dry dislocation is used.

For diffusion, $p = 2.11 \pm 0.15$, $E = 370 \pm 15$ kJ/mol, $A = 10^{7.86 \pm 0.15}$.

For dislocation, $n = 3.64 \pm 0.99$, $E = 424 \pm 23$ kJ/mol, $A = 10^{2.10 \pm 0.20}$.

The mean value is used for each parameter. Preexponential factors *A* listed above are calibrated at 1523 K and 0.3 GPa with activation volume V = 0. We recalibrated the preexponential factor for every activation volume tested in this study as follows:

	A _{diffusion}	A _{dislocation}
$V = 10 \ cm^3$	10 ^{7.78}	10 ^{2.20}
$V = 20 \ cm^3$	10 ^{7.89}	10 ^{2.31}
$V = 30 cm^3$	10 ^{7.99}	10 ^{2.41}

2. SUPPORTING FIGURES

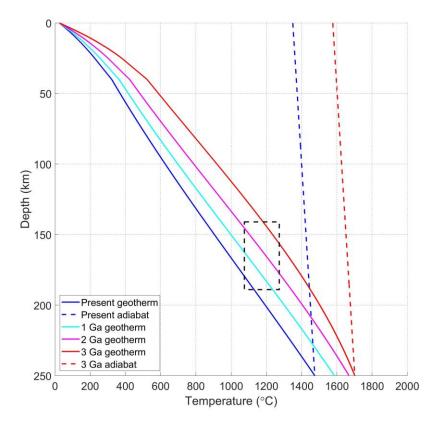


Figure S1. Calculated current, 1 Ga, 2 Ga, and 3 Ga geotherms are plotted with current and 3 Ga adiabat lines. Dashed rectangle represents the constraints from the geothermometry of cratonic diamonds, 1174 ± 99 °C at 55 ± 8 kbar (Stachel and Harris, 2008).

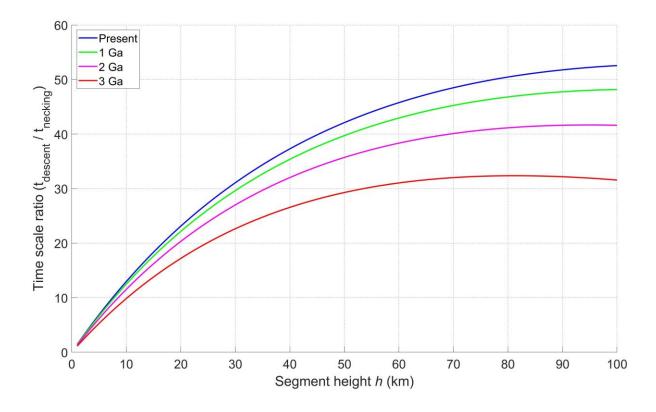


Figure S2. The ratio of the time scale for a segment to descend over the time scale for the growth of necking instability is plotted as a function of segment height *h*. The descent time scale is based on eq. (8) in the main text. The time scale for necking instability is estimated as $t = ((n-1) * \dot{\epsilon})^{-1}$ based on eq. (6) in Zuber and Parmentier (1986). $\dot{\epsilon}$ is the strain rate generated by differential velocity, and *n* is the stress exponent of the material, where we use n = 3.5 for eclogite (Zhang and Green, 2007). Necking instability grows exponentially from infinitesimal perturbations, and segmentation would take place when the ratio >> 1.

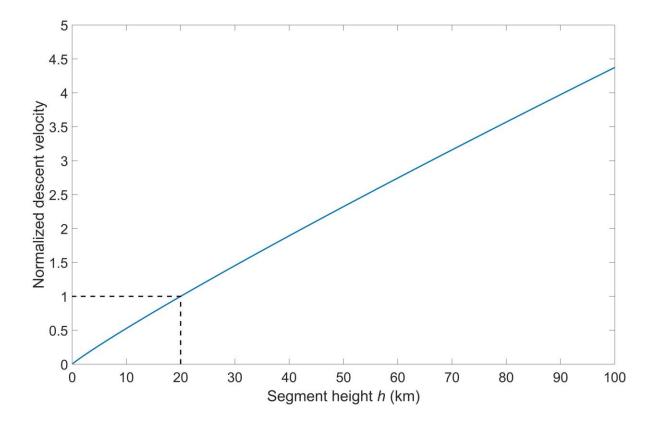


Figure S3. Descent velocities calculated with a range of segment heights are normalized regarding to the result of 20 km height, with other parameters fixed at L = 2500 km, w = 7 km, $\eta = 2 * 10^{30}$ N·m, and $\Delta \rho = 200$ g/cm³.

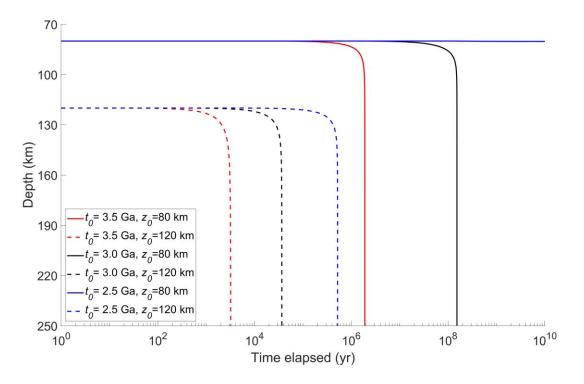


Figure S4. The depth of oceanic crust fragments with different incorporation ages and starting depths is plotted as a function of the time elapsed after incorporated into CLM. An activation volume V of 20 cm³/mol for the dislocation creep regime and a segment height h of 20 km are used for this plot. Each of the curves in this plot corresponds to a point in Figure 3, and the time elapsed until the curst fragments descend to 250 km is the escape time shown in Figure 3.

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